

#### Prince Sultan University STAT 101 Second Examination Second Semester 2010/2011, Term 102 Wednesday, 18<sup>th</sup> May 2011

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# **Time Allowed: 90 minutes**

Maximum points: 40 points

# **Important Instructions:**

- 1. You may use CASIO scientific calculator that does not have programming or graphing capabilities.
- 2. You may NOT borrow a calculator from anyone.
- 3. You do NOT get special consideration if you forget your calculator.
- 4. Don't use notes or any notebook.
- 5. There should be NO talking during the examination.
- 6. Your exam will be taken immediately without any warning if your mobile is seen or heard.
- 7. You must show all your work beside the problem. Be organized.
- 8. You may use the back of the pages for extra space, but be sure to indicate that on the page with the problem.
- 9. This examination has 8 problems, some with several parts. Make sure that your paper has all these problems

| Problem | Max points | Student's Points |  |
|---------|------------|------------------|--|
| 1       | 4          |                  |  |
| 2       | 6          |                  |  |
| 3       | 4          |                  |  |
| 4       | 6          |                  |  |
| 5       | 4          |                  |  |
| 6       | 4          |                  |  |
| 7       | 4          |                  |  |
| 8       | 8          |                  |  |
| Total   | 40         |                  |  |

# Q1 (4 points total)

Let A and B be two independent events such that P(A|B) = 0.2 and  $P(A \cap B) = 0.1$ .

*a.* (2 Points) Calculate  $P(A \cup B)$ .

**b.** (2 Points) Calculate P(B|A).

# *Q2 (6 points)* Circle the right answer in each of the following:

| а. | In how many ways can 4 boys and 3 girls be seated in a row of 7 chairs such that no two of the same sex are set beside each other. |  |                      |                               |  |  |
|----|--|--|----------------------|-------------------------------|--|--|
|    | <b>a.</b> 5040   | <b>b.</b> 144  | <b>c.</b> 12         | <b>d.</b> None of the choices |  |  |
| b. | How many disuch that the   | How many different four-digit numbers can be formed from the digits 1, 2, 3,, 9 such that the first digit is odd, also you can't repeat the digit. |                      |                               |  |  |
|    | <b>a.</b> 336  | <b>b.</b> 120  | <b>c.</b> 1680       | <b>d.</b> None of the choices |  |  |
| с. | The value of   | the permutation  | $_{9}P_{2}$ is equal |                               |  |  |
|    | <b>a.</b> 362880   | <b>b.</b> 36   | <b>c.</b> 72         | <b>d.</b> None of the choices |  |  |

## Q3 (4 points total)

It is reported that 20% of American high school students drop out of school before graduation. Choose 10 students entering high school at random.

- *a.* (2 Points) Find the probability that two drop out of school before graduation.
- *b.* (2 Points) Find the expected number of students who drop out of school before graduation.

## Q4 (6 points total)

Two hundred single-sport athletes were cross-classified according to gender as follows:

Single-Sport Athletes

| Gender | Swimmer | Runner | Cyclist |  |
|--------|---------|--------|---------|--|
| Male   | 25      | 60     | 25      |  |
| Female | 20      | 50     | 20      |  |

An athlete is selected at random.

*a*. (2 Points) What is the probability that the athlete is a runner?

*b*. (2 Points) What is the probability that the athlete is a swimmer and male.

*c*. (2 Points) Given that a randomly selected athlete is a female, what is the probability that she is a runner?

*Q5* (*4 points*) A book shelf has 5 Mathematics books and 4 Statistics books. Four books are chosen randomly one at a time and without replacement. Find the probability of choosing 2 Mathematics books and 2 Statistics books.

**Q6** (*4 points*) The probability that a person will make 0, 1, 2 or 3 errors on his or her income tax return is 0.5, 0.3, 0.15, and 0.05, respectively. If 8 claims are selected, find the probability that 4 will contain 0 errors, 2 will contain 1 error, 1 will contain 2 errors and 1 will contain 3 errors.

**Q7** (4 *points*) If the random variable X has a Poisson distribution with mean  $\lambda = 2$ . Calculate  $P(X \ge 1)$ .

# Q8 (8 points total)

Let X be a random variable with the following probability distribution:

| Х    | -2   | -1   | 0   | 1   | 2   |
|------|------|------|-----|-----|-----|
| P(x) | 0.15 | 0.35 | 0.2 | 0.1 | 0.2 |

- *a.* (2 Points) Calculate P(X > -1).
- *b*. (2 Points) Calculate  $\mu$  (the mean of the random variable X).

*c.* (4 Points) Calculate  $\sigma^2$  (the variance of the random variable X).