

- 1) Consider the vectors  $u = (-2, 4, -8)$ ,  $v = (5, 2, 0)$  and  $w = (4, 1, 8)$ .
- a) Determine whether the angle between  $u$  and  $v$  is acute, obtuse or they are orthogonal.
  - b) Find the vector component of  $u$  along  $w$  and the vector component of  $u$  orthogonal to  $w$ .
  - c) Find a vector orthogonal to both  $u$  and  $v$ .
  - d) Find the norm of  $u + 2v$ .
  - e) Find the volume of the parallelepiped in the 3-space determined by the vectors  $u$ ,  $v$  and  $w$ .

- 2) a) Find the equation of the plane passing through the point  $P(-1, 2, -3)$  and parallel to the plane whose equation is  $2x - 2y + z + 10 = 0$ .
- b) Show that the planes  $3x - 4y + z - 1 = 0$  and  $6x - 8y + 2z - 3 = 0$  are parallel and find the distance between them.
- c) Find parametric equations for the line passing through  $P(3, -1, 2)$  and which is parallel to the vector  $n = (2, 1, 3)$ .
- d) Find the equation of the plane passing through the points  $(1, 1, 1)$ ,  $(2, -1, 3)$  and  $(1, 3, 4)$ .

- 3) Consider the linear operators  $T: R^2 \rightarrow R^2$  and  $S: R^2 \rightarrow R^2$  where  $T$  has the standard matrix representation  $[T] = \begin{bmatrix} 2 & 3 \\ 4 & -1 \end{bmatrix}$  and  $S$  is the rotational operator counterclockwise by an angle  $\frac{\pi}{3}$ .
- a) Is the operator  $T$  one to one ? Onto? Why?
  - b) Find the vector  $v = (ToS)(u)$ , where  $u = (\frac{\sqrt{3}}{2}, 0)$ .
  - c) Find  $T(2,2)$  and  $S(1, -1)$ .
  - d) Find  $(SoT)^{-1}(w)$  if exists, where  $w = (1,1)$ .