

- 1) Consider the vectors $u = (2, -1, 3)$, $v = (1, -3, 4)$ and $w = (2, 2, 1)$.
- a) Find the norm of $u - 2v$ and the distance between u and w .
 - b) Find a vector which is orthogonal to both u and v .
 - c) Calculate the scalar triple product $u \cdot (v \times w)$. What is the volume of the parallelepiped in 3-space determined by the vectors u , v and w .
 - d) Find the cosine of the angle between the vectors u and w .
 - e) Find the vector component of u along v and the vector component of u orthogonal to v .

- 2) a) Find the equation of the plane φ passing through the points $P(2, -1, 4)$, $Q(3, 1, -1)$ and $R(1, 1, 1)$.
- b) Find the parametric equations of the line L passing through $P_1(2, 1, 3)$ and $P_2(1, 2, 2)$,
- c) Find the distance between the line L and the plane φ .

- 3) Consider the linear operators $T: R^2 \rightarrow R^2$ and $S: R^2 \rightarrow R^2$ where T has the standard matrix representation $[T] = \begin{bmatrix} 1 & 3 \\ 3 & 0 \end{bmatrix}$ and S is the rotational operator counterclockwise by an angle $\frac{\pi}{6}$.
- a) Is the operator T one to one ? Onto? Why?
 - b) Find the vector $v = (ToS)(u)$, where $u = (\frac{-1}{2}, \frac{\sqrt{3}}{2})$.
 - c) Find $T(-1,2)$ and $S(1,1)$.
 - d) Find $(SoT)^{-1}(w)$ if exists, where $w = (1,1)$.

- 4) Determine whether the following vectors span \mathbb{R}^3 : $v_1 = (2, -1, 3)$, $v_2 = (4, 1, 2)$, $v_3 = (8, -1, 8)$.