PRINCE SULTAN UNIVERSITY Department of Mathematical Sciences MATH 211 – Business Calculus Final Examination August 2005

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Maximum Time 150 Minutes

- Q1. a. Study the continuity of the function $f(x) = \begin{cases} 2x^2 1 & \text{if } x \ge 1 \\ -x^3 + 2 & \text{if } x < 1 \end{cases}$ at x = 1.
 - b. Find the absolute maximum and absolute minimum of the function $f(t) = 3t^5 5t^3$ on the interval [-3, 1].
 - c. Study the increasing, decreasing and the concavity and use them to sketch the graph of the function $f(x) = x^5 5x^4$.
 - d. Suppose the total revenue in dollars from the sale of q units of a certain commodity is $R(q) = -2q^2 + 68q 128$. At which level of sales is the average revenue equals the marginal revenue?
- Q2. a. How much money should be invested today at 5 percent compounded continuously so that 10 years from now it will be worth \$10,000
 - b. A manufacturer can produce toasters at a cost of \$7 apiece and estimates that if they are sold for x dollars apiece, consumers will buy approximately $2,000e^{-0.2x}$ toasters per week. At what price should the toasters be sold in order to maximize profit?
 - c. Find the derivative of the following functions

$$y = \frac{2x-4}{x^2-2}$$

$$y = x^2 e^{4x}$$

$$y = \ln\left(\frac{x^2(2x-3)^4}{\sqrt{x-1}}\right)$$

Q3. Evaluate the following integrals

a.
$$\int \frac{x \, dx}{\sqrt{x^2 + 1}}$$

b. $\int_0^1 (x^3 - 3x^2 + 5) \, dx$
c. $\int \frac{2x - 3x^4 e^{2x}}{x^4} \, dx$
d. $\int \left(5e^2 - \frac{3}{x^5} + \frac{5}{x} \right) \, dx$

- Q4. a. Find the function whose tangent line has the slope $3x^2 + 1$ for each value of x and whose graph passes through (0, 2).
 - b. Determine the area of the region bounded by the curves $y = 1 + 4x x^2$ and $y = 1 + x^2$.
 - c. At a certain factory, the marginal cost is $3(q-4)^2$ dollars per unit when the level of production is q units.
 - 1. What is the cost of producing 14 units if the overhead is \$436?
 - Use the marginal cost to estimate the cost of producing the 14th unit and compare it with the actual cost of producing the 14th unit.
 - ". By how much will the total cost increase if the level of production is raised from 6 units to 10 units?