

Prince Sultan University Department of Mathematics and Physical Sciences

Math 113 Final Exam

Semester I, Term 131 Thursday, January 2, 2014

Time Allowed: 120 minutes

Name:
Student Number:

Statement of Ethics:

Instructor's Name:

I agree to complete this exam without unauthorized assistance from any person, materials, or device.

Signature:

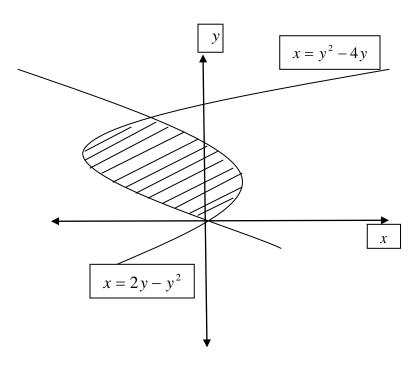
Total/80:

Total/40:

Q.1 (4 points) Find the second derivative (y'') of the function $y = \int_{0}^{3x^2+1} \sin(t) dt$.

Q.2 (3 points) Write down the partial fraction decomposition of the function $\frac{x^2-2x-1}{(x-1)^2(x^2+1)}$ without the determination of the coefficients.

Q.3 (5 points) Find the area of the shaded region:





Q.4 (4 points) Use the method of the cylindrical shells to find the volume generated by rotating the region bounded by the curves $y=x^2$ and $y=2-x^2$ about x=1. Set up the integral and do not evaluate it.

Q.5 ((a): 4 points, (b): 6 points, (c): 4 points, (d): 4 points) Evaluate the integrals:

a)
$$\int (2x-3)(4x^2+x^{\frac{1}{2}})dx$$

$$b) \int \frac{\sqrt{x^2 - 9}}{x^3} dx$$

c)
$$\int \frac{(x-1)e^x}{x^2} dx$$
 (Hint: Use integration by parts).

d)
$$\int_{0}^{\pi/3} \tan^5 x \sec^4 x dx$$

Q.6 ((a):5 points, (b): 4 points) **Determine whether the integrals are convergent or divergent. If they converge evaluate them:**

a)
$$\int_{0}^{\infty} \frac{x^2}{\sqrt{1+x^3}} dx$$

b)
$$\int_{2}^{\infty} xe^{-3x} dx$$

Q.7 (5 points) Find the exact length of the curve $y=2(x+4)^{\frac{3}{2}},\ 0\leq x\leq 2,\ y>0.$

Q.8 ((a): 5 points, (b): 6 points, (c): 4 points, (d): 5 points) **Test the series for convergence and divergence:**

$$a) \quad \sum_{n=1}^{\infty} \frac{\sin 2n}{1+2^n}$$

b)
$$\sum_{n=1}^{\infty} (-1)^n \frac{\sqrt{n}}{2n+3}$$

c)
$$\sum_{n=1}^{\infty} \frac{n^2 - 5n}{n^3 + n + 1}$$

$$d) \quad \sum_{n=1}^{\infty} \frac{e^{\frac{1}{n}}}{n^2}$$

Q.9 (5 points) Determine whether the series $\sum_{n=1}^{\infty} \left(\frac{-2n}{n+1}\right)^{5n}$ is absolutely convergent, conditionally convergent or divergent.

Q.10 (7 points) Find the radius and interval of convergence of the series $\sum_{n=1}^{\infty} \frac{(2x-1)^n}{5^n \sqrt{n}}$.