PRINCE SULTAN UNIVERSITY	Prince Sultan Universi MATH 111 Major Test I Semester I, Term 151 Monday, October 19, 2015	ty Time Allowed: <u>90 minutes</u>
Student Name:		
Student ID #:		
Teacher's Name: _		_Section #:

Serial #: _____

Important Instructions:

- 1. You may use a scientific calculator that does not have programming or graphing capabilities.
- 2. You may NOT borrow a calculator from anyone.
- 3. You may NOT use notes or any textbook.
- 4. There should be NO talking during the examination.
- 5. Your exam will be taken immediately if your mobile phone is seen or heard
- 6. Looking around or making an attempt to cheat will result in your exam being cancelled
- 7. This examination has 11 problems, some with several parts. Make sure your paper has all these problems.

Problems	Max points	Student's Points
1,2,3,4	19	
5	25	
6,7,8	20	
9,10,11	16	
Total	80	

Q1. (2 points) Find the domain of the function $F(x) = \sqrt[3]{5 - |x|}$

Q2. (4 points) Graph the function by starting with standard function and using transformation: $y = \left|\sqrt[3]{x} - 1\right|$



Q3. (5 points) Show that the equation $\sin x = x^2 - x$ has a root in the interval (1, 2).

Q4. (8 points) Find the horizontal and vertical asymptotes of each curve: (Show your work in details) 1 - n = 1

1.
$$y = \frac{1}{\sqrt{e^x - 1}}$$

2.
$$y = \frac{1+x^4}{x^2 - x^4}$$

Q5. (25 points) Evaluate the limit, if it exists. (Show your work in details) $r^2 = r^2$

1.
$$\lim_{x \to 3} \frac{x^2 - x - 6}{|x - 3|}$$

2.
$$\lim_{x \to \infty} \frac{2 - 3x^3}{6x^3 + 5000x + 100}$$

3.
$$\lim_{x \to -\infty} \frac{e^{3x} - e^{-3x}}{e^{3x} + e^{-3x}}$$

4.
$$\lim_{x \to \infty} \frac{\cos x}{x^2 + 1}$$

5.
$$\lim_{x \to 1} \frac{x^2 - 1}{\sqrt{x + 3} - 2}$$

Q6. (4 points) Use the graph of the function to find the following:

- a) $\lim_{x \to 2} f(x)$ b) $\lim_{x \to -1^-} f(x)$ c) $\lim_{x \to \infty} f(x)$ d) $\lim_{x \to -\infty} f(x)$
- Q7. (8 points) a. Use the definition to find the derivative of the function $y = 3x x^2$.

- b. Find the equation of the tangent line at x = 4.
- Q8. (8 points) Find the value of "a" and "b" that makes the function continuous everywhere.

$$f(x) = \begin{cases} \frac{x^2 - 1}{x + 1} & x < 1\\ ax^2 - bx - 1 & 1 \le x < 2\\ x - 2a + b & x \ge 2 \end{cases}$$

Q9. (6 points) a. Prove that if a function f(x) is differentiable at x = a, then it is continuous at x = a.

b. Give a counter example where the converse is not true (Justify your answer)

Q10. (5 points) Find $\lim_{x \to -\infty} \sqrt{x^2 - 2} + x$

Q11. (5 points) Find
$$\lim_{x \to \infty} f(x)$$
, if for all $x > 1$, $\frac{10e^{x} - 21}{2e^{x}} \le f(x) \le \frac{5\sqrt{x}}{\sqrt{x-1}}$.