

Prince Sultan University Orientation Mathematics Program MATH 001 Midterm Examination Semester I, Term 091 Monday, December 7, 2009 Time Allowed: 90 minutes $(1\frac{1}{2}hour)$

Student Name: ______

Student ID #: _____

Section #: _____

Teacher's Name: _____

Important Instructions:

- 1. You may use a scientific calculator that does not have programming or graphing capabilities.
- 2. You may NOT borrow a calculator from anyone.
- 3. You may NOT use notes or any textbook.
- 4. There should be NO talking during the examination.
- 5. Your exam will be taken immediately if your mobile phone is seen or heard
- 6. Looking around or making an attempt to cheat will result in your exam being cancelled
- 7. This examination has 13 problems, some with several parts. Make sure your paper has all these problems.

Problems	Max points	Student's Points	
1,2,3,4	17		
5,6,7,8	24		
9	16		
10,11	17		
12	16		
13	10		
Total	100		

Show all steps for each question

Q.1 (4 points) Evaluate the algebraic expression for the given values of the variables.

$$\frac{|y|-7|x|}{6x+xy}$$
, for $x = -1$ and $y = 3$.

Q.2 (2 points) Find the intersection of the two sets. $\label{eq:constraint} \{2,3,5,9\} \cap \{5,11,2\}$

Q.3 (2 points) List all numbers from the given set B that are members of the subset of <u>Natural Numbers.</u> $B = \{6, \sqrt{5}, -12, 0, 0.\overline{1}, \sqrt{9}\}$

- Q.4 (9 points) Simplify each of the following expressions. Assume that all variables represent positive numbers.
 - (i) $(4x^{-4}y^{8})(2xy^{6})$
 - (i) $16x^2 + 2 \left[4\left(x^2 6\right) + 9\right]$

(iii)
$$\sqrt{3x} - 7\sqrt{27x} + 6\sqrt{75x}$$

Q.5 (4 points) Rationalize the denominator in $\frac{5}{6-\sqrt{3}}$

Q.6 (5 points) Simplify the rational expression. Find all numbers that must be excluded from the domain of the rational Expression

$$\frac{4y^2 - 7y - 2}{y^2 - 3y + 2}$$

Q.7 (8 points) Perform the indicated operations and write the result in standard form.

(i)	$\left(2-\sqrt{-9}\right)^2$
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(ii)
$$\frac{4i}{3-2i}$$

- Q.8 (7 points) Consider the equation y = -2x+1.
 - (i) Graph this equation. Select integers for *x*, starting with -2 and ending with 2.

x	-2	-1	0	1	2
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- (ii) Determine the x-intercepts, if any.
- (iii) Determine the y-intercept, if any.



Q.9 (16 points) Perform the indicated operations and simplify as much as possible.

(i)
$$(5x^4y^2 + 9x^3y - 10y) - (3x^4y^2 + 7x^3y + 2y - 10x)$$

(ii)
$$(2x-1)(2x+1)(x^2+3)$$

(iii)
$$\frac{x^2 - 81}{2x - 2} \div \frac{x^2 + 18x + 81}{x^2 + 8x - 9}$$

(iv)
$$\frac{3}{x+2} - \frac{x-10}{x^2-4}$$

Q.10 (12 points) Factor each of the following <u>completely</u>:

(i) $25x^2 - 9$

(iii) $9x^4 - 9x$

(iv) $x^3 + 4x^2 - 16x - 64$

(v)
$$(x^2+2)^{-\frac{2}{3}}+(x^2+2)^{-\frac{5}{3}}$$

Q.11 (5 points) Find all values of x satisfying the given conditions.

$$y_1 = \frac{x-3}{5}$$
, $y_2 = \frac{x-5}{4}$, and $y_1 - y_2 = -4$

Q.12 (16 points) Solve each of the following equations.

(i) 3(x-4)-4(x-3)=x+3-(x-4)

(ii)
$$x^2 + x - 1 = 0$$

(iii)
$$(x-1)^{\frac{3}{4}} - 8 = 0$$

(iv)
$$\sqrt{2x+18} = x+5$$

Q.13 (10 points) Solve each of the following inequalities and *graph* the solution set on a number line. Express the solution set using *interval notation*.

(i) 9x+1 > 3(2x+1)+4

(ii) $3|7-2x| \le 27$