

Prince Sultan University Orientation Mathematics Program MATH 001 Midterm Examination Semester I, Term 081 Sunday, November 30, 2008 Time Allowed: 90 minutes

Student Name:	
Student ID #:	Section #:

Teacher's Name: \_\_\_\_\_

## Important Instructions:

- 1. You may use a scientific calculator that does not have programming or graphing capabilities.
- 2. You may **NOT borrow** a calculator from anyone.
- 3. You may NOT use notes or any textbook.
- 4. There should be **NO talking** during the examination.
- 5. Your exam will be taken **immediately** if your mobile phone is seen or heard
- 6. Looking around or making an attempt to cheat will result in your exam being cancelled
- 7. Provide an organized complete solution for each Question.
- 8. This examination has 12 problems. Make sure your paper has all these problems.

Problems	Max points	Student's Points
1	12	
2, 3	22	
4	16	
5, 6, 7	18	
8, 9, 10	13	
11,12	19	
Total	100	

- 1. (12 points) Simplify each of the following expressions
  - i.  $14x^2 + 5 \left[7(x^2 2) + 4\right]$

ii. 
$$(125x^9y^6)^{\frac{1}{3}}$$

iii. 
$$\left(\frac{x^4y^5z^6}{x^{-4}y^{-5}z^{-6}}\right)^{-4}$$

iv. 
$$\frac{\sqrt[4]{162x^5}}{\sqrt[4]{2x}}$$

2. (6 points) Evaluate the following:

i. 
$$\sqrt[3]{\sqrt[4]{16} + \sqrt{625}}$$

ii. 
$$\frac{|x|}{x} - \frac{|y|}{y}$$
 for  $x = 2$  and  $y = -5$ .

3. (16 points) Factor each of the following completely i.  $81x^4 - 1$ 

ii. 
$$2x^2 + 5x - 3$$

iii. 
$$(x^2+3)^{-\frac{2}{3}}+(x^2+3)^{-\frac{5}{3}}$$

iv.  $x^2 y - 16y + 32 - 2x^2$ 

4. (16 points) Perform the indicated operations and simplify:

i.  $3\sqrt{54} - 2\sqrt{24} - \sqrt{96} + 4\sqrt{63}$  (Note: Show all your steps)

ii. 
$$(x+9y)(6x+7y)$$

iii. 
$$(7x^4y^2 - 5x^2y^2 + 3xy) + (18x^4y^2 - 6x^2y^2 - xy)$$

iv. 
$$\frac{x^2 + x - 12}{x^2 + x - 30} \cdot \frac{x^2 + 5x + 6}{x^2 - 2x - 3} \div \frac{x + 3}{x^2 + 7x + 6}$$

5. (3 points) Find all numbers that must be excluded from the domain of  $\frac{x-3}{x^2+4x-45}$ .

6. (3 points) Rationalize the denominator of:  $\frac{11}{\sqrt{7} - \sqrt{3}}$ . (Note: Show all your steps)

7. (12 points) Solve the following inequalities. Express the solution using interval notation.

i. 
$$-4(x+2) > 3x+20$$

ii. 
$$-6 \le \frac{1}{2}x - 4 < -3$$

iii. 
$$\left|3-\frac{2}{3}x\right| > 5$$

8. (5 points) Graph  $y = 2x^2 - 4$ . Determine the *x* – intercept and the *y* – intercept.



9. (4 points) Write the expression  $\sqrt{-8}(\sqrt{-3} - \sqrt{5})$  in the standard form of a complex number. (Note: Show all your steps)

10. (4 points) Evaluate  $\frac{x^2 + 11}{3 - x}$  for x = 4i.

- 11. (15 points) Find the solution set of each equation
  - i.  $3(x-4)^2 = 15$

ii.  $x^2 + 4x + 1 = 0$ 

iii. 
$$\sqrt{2x+15} - 6 = x$$

12. (4 points) Given  $y_1 = \frac{x+1}{4}$  and  $y_2 = \frac{x-2}{3}$ . Find all values of x satisfying  $y_1 - y_2 = -4$ .