



Prince Sultan University  
Department of Mathematical Sciences

**Major II Exam**

Semester II, 2007 SPRING (062)

18<sup>th</sup> April, 2007

**MATH 113 – CALCULUS II**

Time Allowed : 90 minutes

Maximum Points: 50 points

**Mr. Khaled Naseralla**

Name of the student : \_\_\_\_\_

ID number : \_\_\_\_\_

Section : \_\_\_\_\_

**For All The Students:**

- Answer all the questions.
- This exam consists of **a total of 6 pages and 7 questions.**
- Show your working in the space provided for each question.
- Show all the key steps of your work.
- Scientific, non-programmable calculators are allowed.

Question	Maximum score	<i>Your Score</i>
Q.1	15	
Q.2	5	
Q.3	6	
Q.4	6	
Q.5	5	
Q.6	5	
Q.7	8	
<b>Total</b>	<b>50</b>	

**Q.1** : Evaluate the following integrals:

(3 points each)

a)  $\int_1^4 \frac{1}{\sqrt{x}(1+\sqrt{x})} dx$

b)  $\int \frac{e^{2t}}{\sqrt{e^{2t}-4}} dt$

c)  $\int \frac{\sin(\ln x^3)}{x} dx$

d)  $\int_0^1 \frac{e^x - 1}{e^{2x}} dx$

e)  $\int \frac{x}{1 + x \tan x} dx$

**Q.2:** Find the area of the region bounded by  $y = 2x - 2$  and  $x = \frac{1}{2}y^2$  (5 points)

**Q.3:** Find the arc length of the graph of  $f(x) = x^{\frac{3}{2}} + 1$  for  $0 \leq x \leq \frac{4}{3}$

**(6 points)**

**Q.4:** Find the area of the surface generated when  $y = \sqrt{1-x^2}$  on the interval  $\left[0, \frac{1}{2}\right]$  is revolved about  $x$ -axis

**(6 points)**

**Q.5:** Use the cylindrical shell method to find the volume of the solid generated when the region bounded by the graphs of  $y = x^2 + 3$  and  $x = y - 5$  is revolved around  $y$ -axis (5 points)

**Q.6:** Use the washers method to find the volume of the solid generated when the region bounded by  $y = 4\sqrt{x}$ ,  $y = 4$ ,  $x = 4$  and  $x = 9$  is revolved about  $x$ -axis (5 points)

- Q.7:** Let  $R$  be the region between the graphs  $y = 2x$  and  $y = x^2$  (8 points)  
Find the volume of the solid generated by revolving  $R$  about:
- a)  $x$ -axis
  - b) the line  $x = -2$