



Prince Sultan University
Department of Mathematical Sciences
Major I Exam

Semester I, FALL 2009 (091)
2nd November, 2009

MATH 113 – CALCULUS II

Time Allowed : 90 minutes

Maximum Points: 100 points

Mr. Khaled Naseralla

Name of the student : _____

ID number : _____

Section : **221** _____

For All The Students:

- Answer all the questions.
- This exam consists of **a total of 6 pages and 11 questions.**
- Show your working in the space provided for each question.
- Show all the key steps of your work.
- Scientific, non-programmable calculators are allowed.

Question	Maximum score	Your Score
1 , 2	42	
3 , 4 , 5 , 6	24	
7 , 8	13	
9 , 10 , 11	21	
Total	100	

15

Q.1 (36 points) : Evaluate the following integrals. **(Show your work)**

a) $\int_{-5}^5 f(x)dx$ if $f(x) = \begin{cases} x^3 & \text{if } x > 1 \\ 5 - x^2 & \text{if } x \leq 1 \end{cases}$

b) $\int x^2 (x^3 + 9)^8 dx$

c) $\int \cos^4(3t) \sin(3t) dt$

d) $\int_1^3 x^3 (2x + \frac{1}{x^4}) dx$

e) $\int \frac{3x + 6}{2x^2 + 8x + 3} dx$

f) $\int \frac{\cos 3x}{\sqrt{5 + 2\sin 3x}} dx$

Q.2 (6 points): Suppose that $F(x)$ is a continuous function and suppose that $F(-1) = 3$, $F(3) = 5$, $F'(-1) = 2$ and $F'(3) = -2$. Find the following:

a) $\int_{-1}^3 F'(x) dx$

b) $\int_{-1}^3 F''(x) dx$

c) $\int_{-1}^3 [F(x)]^2 \cdot F'(x) dx$

Q.3 (6 points): Let $F(x) = \int_4^x (10t^2 + \sqrt{t}) dt$ Find

a) $F(4)$

b) $F'(4)$

c) $F''(4)$

Q.4 (4 points): Given $\int_6^8 f(x) dx = 3$, $\int_8^{20} f(x) dx = 7$ and $\int_6^{20} g(x) dx = 8$
Find $\int_6^{20} [6f(x) + g(x)] dx$

Q.5 (6 points): Evaluate $\sum_{k=1}^{12} k(3k + 2)$

Q.6 (8 points): Use the limit of the **Riemann Sum** to find the area under the curve $f(x) = 5 - 2x$ over the interval $[0, 1]$, using x_k^* as the right endpoint of each subinterval.

Q.7 (8 points): The velocity of an object moving along an S -axis is given by: $v(t) = (2t^3 - 2t) \text{ m/s}$

i) Find the total distance the object travels over the period $0 \leq t \leq 4$

ii) Find the position of the object at $t = 3$ seconds given that $S(0) = -3$

iii) Find the acceleration of the object at $t = 2$ seconds

Q.8 (5 points): A ball is fired vertically upward from ground level with an initial velocity 64 ft/s . Determine the maximum height the ball reaches.

$$\begin{aligned} S &= S_0 + V_0 t - \frac{1}{2} g t^2 \\ V &= V_0 - g t \\ g &= -32 \text{ ft/s}^2 \text{ or} \\ g &= -9.8 \text{ m/s}^2 \end{aligned}$$

Q.9 (7 points): Find the value(s) of x^* that satisfies the Mean-Value Theorem for the function $f(x) = 3x + 1$ on the interval $[0, 6]$

Q.10 (6 points): Solve the initial value problem:
$$\frac{dy}{dx} = \cos x - 5x \quad , \quad y(0) = 4$$

Q.11 (8 points): Use the definite integral to find the area between $f(x) = |x - 1| + 2$ and the x -axis over the interval $[0, 5]$. Sketch the graph of $f(x)$ to verify the area using geometric formula.