

**PRINCE SULTAN UNIVERSITY****MATH 111****CALCULUS****MAJOR EXAM 3****14<sup>th</sup> JANUARY 2009****Time allowed: 50 minutes****Name:** \_\_\_\_\_**I.D.** \_\_\_\_\_**Instructors Name:** \_\_\_\_\_**Section:** \_\_\_\_\_

1. Answer all questions
2. This exam consists of 1 Cover Sheet & 2 Question Sheets with 4 questions.
3. You can use a calculator, **NOT** a mobile phone.
4. No talking during the test.
5. Show all working out in the space provided.

Question No.	Max. Points	Points Scored
1	15	
2	5	
3	5	
4	5	
<b>TOTAL SCORE</b>	<b>30</b>	

**1)** [15 points] Find  $\frac{dy}{dx}$

(a)  $y = (x^2 + 2x - 1)^5 + \sqrt[3]{\tan x}$

(b)  $y = \frac{e^{3x}}{\ln x}$

(c)  $y = x^2 \log_2(3 - 2x)$

(d)  $y = \sin^2(e^x) + 3^{-x}$

(e)  $y = x \sin^{-1} x + \sqrt{1 - x^2}$

**2)** [5 points] Find the equation of the tangent line to the curve  $xy + y^2 = 2$  at the point  $(1, 1)$ .

**3)** [5 points] Given that  $y = \frac{x \cos^3(x) \tan^{-1} x}{\sqrt{2x+1}}$ . Use logarithmic differentiation to find  $y'$ .

**4)** [5 points] A 10-ft ladder is leaning against a vertical wall. If the bottom of the ladder is pulled along the ground away from the wall at a constant rate of 2 ft/s, how fast will the top of the ladder be moving down the wall when the top is 6 ft above the ground?.