

- 1) Consider the vectors $u = (1, -2, 3)$ and $v = (1, -2, 4)$.
- a) Find $\|u + v\|$.
 - b) Find the vector component of u along v **and** the vector component of u orthogonal to v .
 - c) Find cosine of the angle between u and v .

- 2) Find the distance between the point $P(1,1,1)$ and the plane passing through the points $P_1(2,0,3)$, $P_2(-1,1,3)$ and $P_3(0,1,2)$.

- 3) a) Find parametric equations for the line of intersection of the planes :
 $x - 2y + 3z = -2$ and $-3x + y + 2z + 5 = 0$.
- b) Find an equation for the plane passing through $P(-2,1,7)$ that is perpendicular to the line $x - 4 = 2t, y + 2 = 3t, z = -5t, -\infty < t < \infty$.

- 4) Consider the linear operators $T: R^2 \rightarrow R^2$ and $S: R^2 \rightarrow R^2$ where T has the standard matrix representation $[T] = \begin{bmatrix} 1 & 3 \\ 3 & 0 \end{bmatrix}$ and S is the rotational operator counterclockwise by an angle $\frac{\pi}{3}$.
- a) Is the operator T one to one ? Onto? Why?
 - b) Find the vector $v = (T \circ S)(u)$, where $u = (\frac{-1}{2}, \frac{\sqrt{3}}{2})$.
 - c) Find $T(-1, 2)$ and $S(1, 1)$.
 - d) Find $(S \circ T)^{-1}(w)$ if exists, where $w = (1, 1)$.