



PrinceSultanUniversity  
Math113, Major Exam 1  
Term 182

Time Allowed: 75 minutes

Student Name: \_\_\_\_\_

Student ID #: \_\_\_\_\_

Serial Class #: \_\_\_\_\_

Section #: \_\_\_\_\_

Instructor's Name: \_\_\_\_\_

**Important Instructions:**

1. You may use a scientific calculator that does not have programming or graphing capabilities.
2. You may NOT borrow a calculator from anyone.
3. You may NOT use notes or any textbook.
4. Talking during the examination is NOT allowed.
5. Your exam will be taken immediately if your mobile phone is seen or heard.
6. Looking around or making an attempt to cheat will result in your exam being cancelled.
7. This examination has 6 problems, some with several parts. Make sure your paper has all these problems.

Problems	Max marks	Student's marks
Q#1, Q#2	10	
Q#3	16	
Q#4,Q#5	8	
Q#6	6	
Total	40	

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**Q1) [6 Marks]** Use the definition of the integral to find the integral  $\int_0^2 x^2 dx$ .

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**Q2) [4 Marks]** If  $\int_0^6 f(x)dx = 10$  and  $\int_0^4 f(x)dx = 7$ , find  $\int_4^6 f(x)dx$ .

**Q3) [16 Marks]** Find the following integrals

a)  $\int_1^6 \frac{\sqrt{x}-3x^2}{x} dx$

b)  $\int_0^1 \frac{e^x}{1+e^{2x}} dx$

c)  $\int (1 + \tan \theta)^3 \sec^2 \theta d\theta$

d)  $\int_{-1}^4 |x-2| dx$

Q4) [3 marks] Find the derivative of the function  $f(x) = \int_0^{x^2} \sqrt{\cos t} \, dt$ .

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Q5) [5 Marks] Sketch the region enclosed by the curves  $x = 2y^2$ ,  $x = 4 + y^2$  and find its area.

**Q6) [6 Marks]** Find the volume of the solid obtained by rotating the region bounded by the curves  $y = e^x$ ,  $y = 0$ ,  $x = -1$ ,  $x = 1$  about the  $x$ -axis.