## Prince Sultan University, Department of Mathematics, 6/11/10. Calculus II (Math 113), Mid-Term 2- Fall (101).

Duration: 90 min

Dr Abdul-Wahed HAMDI

- Answer all the questions.
- This exam consists of a total of 4 pages and 5 questions.
- Show your working in the space provided for each question.
- Show all the key steps of your work.
- Scientific, non-programmable calculators are allowed.

Question	Maximum Score	Your Score
1	12	
2	12	
3	5	
4	5	
5	16	
Total	50	

Name	
ID Number	

1. Determine 
$$\frac{dy}{dx}$$
(a)  $y = \frac{x^2}{1 + \log_2(x)}$ 

(b) 
$$y = \frac{\sin(x)\tan^2(x)\cos(x)}{\sqrt{2-x}}$$

(c) 
$$y = \log_x(2)$$
.

(d) 
$$y = [\sin(2x)]^{2x^3 - 2x}$$

2. Evaluate the following definite integrals

(a) 
$$\int_{e^{-3}}^{e^3} \frac{\sqrt{9 - (\ln(x))^2}}{x} dx$$

(b) 
$$\int_{-1}^{1} \sqrt{e^{3x}} dx$$

(c) 
$$\int_{-1}^{1} \frac{e^{-2x} + e^{2x}}{e^{-2x} - e^{2x}} dx.$$

**3.** Find the exact arc length of the curve  $x = (y^2 + 2)^{3/2}$  from y = 0 to y = 1.

4. Determine the surface area of the solid obtained by revolving  $y = \sqrt{4 - x^2}$ ,  $x \in [-1, 1]$  about the x-axis.

- 5. Setup the integral giving the volume by two methods (Cylindrical Shells and Washers) of the solid generated by revolving the region bounded by:

  - (a)  $y=0, y=\sqrt{x+1}, x=8$  about the line x=-3 (b)  $y=x^2-5x+4$  and the x-axis about the line y=-4