

### COURSE DETAILS:

ORIENTATION MATHEMATICS I		MATH 001	FINAL EXAM A
Semester:	Fall Semester --Term 191		
Date:	Saturday December 14, 2019		
Time Allowed:	120 minutes (2 hours)		

### STUDENT DETAILS:

Student Name:	
Student ID Number:	
Section:	
Instructor's Name:	

### INSTRUCTIONS:

- You may use a scientific calculator that does not have programming or graphing capabilities. NO borrowing calculators.
- NO talking or looking around during the examination.
- NO mobile phones. If your mobile is seen or heard, your exam will be taken immediately.
- Show all your work and be organized.
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### GRADING:

	Page 1	Page 2	Page 3	Page 4	Page 5	Total	Total
Questions							
Marks	10	10	24	19	17	80	40

**Q.1A (20 points) Choose the correct answer**

1) Find the **distance** between the two points:  $(4, -6)$  and  $(5, 2)$

A) distance  $= \sqrt{17}$

B) distance  $= \sqrt{97}$

C) distance  $= \sqrt{65}$

D) distance  $= \sqrt{63}$

2) Let  $f(x) = \frac{2}{x-6}$  and  $g(x) = \frac{x}{x+1}$ , then the **domain** of  $(f+g)(x)$  is:

A)  $[-1, 6]$

B)  $\mathbb{R} - \{-1, 6\}$

C)  $(-1, 6)$

D)  $\mathbb{R} - \{-1, 0, 6\}$

3) Find the **x-intercepts** of the graph of the equation:  $y = (x+4)^2 - 1$

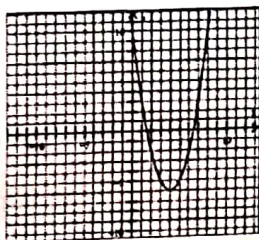
A)  $\{3, 5\}$

B)  $\{-5, -3\}$

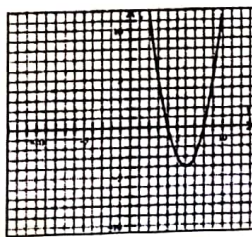
C)  $\{-3\}$

D)  $\{-4, 1\}$

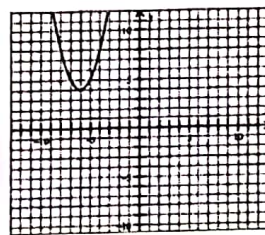
4) Use the graph of  $f(x) = x^2$  and the transformations to obtain the graph of  $g(x) = (x-4)^2 - 6$ :



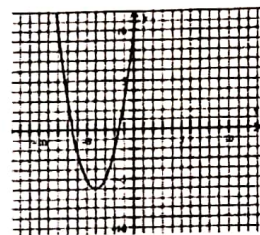
A)



B)



C)



D)

5) Factor completely.  $y^5 - 16y$

A)  $y(y-2)(y+2)(y^2+4)$

B)  $y(y-4)^2(y+4)^2$

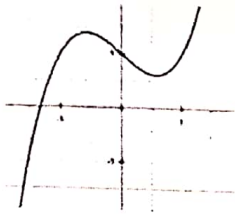
C)  $y^2(y^2-8y+16)$

D)  $y(y^4-8y^2+16)$

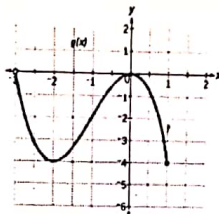
*You must write the correct answer to each question in the box below*

Question	1	2	3	4	5
Answer					

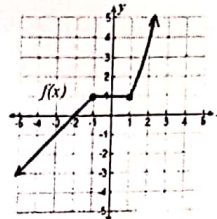
6A) Which of the following is a graph of a **one-to-one function**?



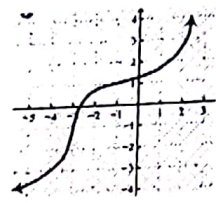
A)



B)



C)



D)

7) Find the equation of the circle with center  $(-2, 3)$  and radius 5

A)  $(x+2)^2 + (y-3)^2 = 5$

B)  $(x-2)^2 + (y+3)^2 = 25$

C)  $(x+2)^2 + (y-3)^2 = 25$

D)  $(x-2)^2 - (y+3)^2 = 25$

8)  $\left(\frac{x^{-6}y^4}{x^2y^{-1}}\right)^{-2} =$

A)  $\frac{x^8}{y^6}$

B)  $\frac{y^{10}}{x^{16}}$

C)  $\frac{x^{16}}{y^{10}}$

D)  $\frac{y^6}{x^8}$

9) Find the solution set of the inequality:  $|x-2|+4=10$

A)  $\{-6, 6\}$

B)  $\{4\}$

C)  $\{-8, 4\}$

D)  $\{-4, 8\}$

10) Find the solution set of the inequality:  $x(x-3) < 0$

A)  $(3, \infty)$

B)  $(-\infty, 0) \cup (3, \infty)$

C)  $(0, 3)$

D)  $(-\infty, 3)$

*You must write the correct answer to each question in the box below*

Question	6	7	8	9	10
Answer					

**Q.2A (3+3+4 points):** Perform the indicated operations and **simplify**.

a)  $(4x-3)^2$

b)  $\sqrt{3x^3} \cdot \sqrt{8x^2}$

c)  $\frac{x^2-5x-6}{x} \div \frac{x^2-36}{x+6}$

**Q.3 (6 points):** Find an equation in of the line that passes through  $(1, -2)$  and is **perpendicular** to the line passing through  $(3, 4)$  and  $(0, 6)$

**Q.4 (8 points):** Solve the following equations. Give the solution set. **(Don't use a calculator)**

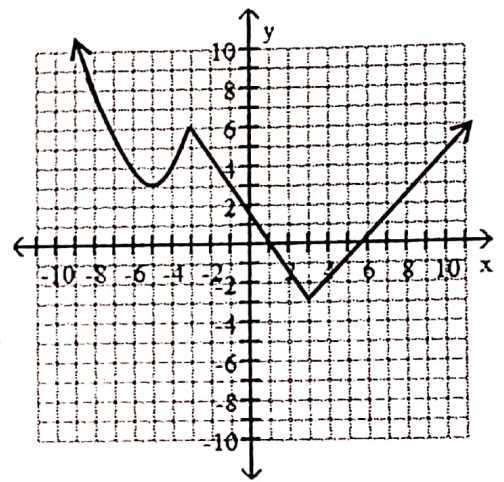
a)  $2(1-x) = 3(1+2x) + 15$

b)  $4x^2 - 3x = 7$

**Q.5A (4 points):** Find the inverse function,  $f^{-1}(x)$  for  $f(x) = 3 + \sqrt{x+2}$  ;  $x$  is positive

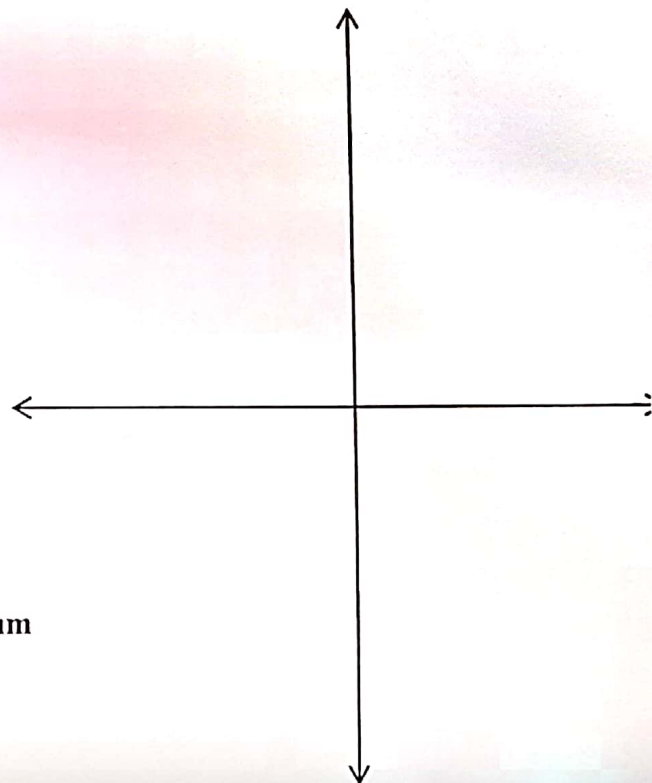
**Q.6 (6 points):** Use the graph  $f$  to find each of the following.

- The **range** of  $f$
- Intervals where the graph is **increasing**
- Coordinates of the local maximum**
- The **values of  $x$**  for which  $f(x) = 0$
- $f^{-1}(6) =$



**Q.7 (9 points):** Consider the quadratic function  $f(x) = -x^2 + 4x + 5$

- Find the **vertex** of  $f$
- Find the  $x$ -intercepts, if any
- Find the  $y$ -intercept
- Determine whether  $f$  has a **maximum** or a **minimum**



**Q.8A (5 points):** Find all the zeros of  $P$  (real and complex).  $P(x) = x^4 + 3x^2 - 4$   
(Don't use a calculator)

**Q.9 (6 points):** Use the Synthetic division to show that  $x = 3$  is a zero of  $P(x) = x^3 - x^2 - 11x + 15$ , then find all other zeros of  $P$ .  
(Show all your steps and don't use a calculator)

**Q.10 (6 points):** Find a fourth – degree polynomial that has  $-1, 1, 3$  and  $5$  as zeros.  
(Simplify as much as possible)

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**Q.1B (20 points)** Choose the correct answer

1) Factor completely.  $y^5 - 16y$

A)  $y(y^4 - 8y^2 + 16)$

B)  $y^2(y^2 - 8y + 16)$

C)  $y(y-4)^2(y+4)^2$

D)  $y(y-2)(y+2)(y^2+4)$

2) Find the solution set of the inequality:  $|x-2|+4=10$

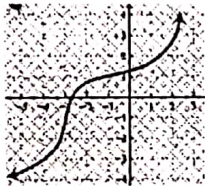
A)  $\{-4, 8\}$

B)  $\{-8, 4\}$

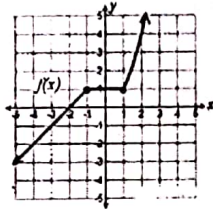
C)  $\{4\}$

D)  $\{-6, 6\}$

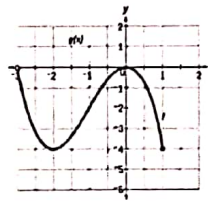
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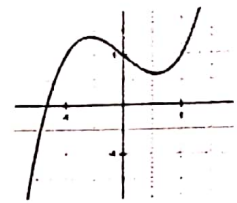
A)



B)



C)



D)

4) Find the solution set of the inequality:  $x(x-3) < 0$

A)  $(-\infty, 0) \cup (3, \infty)$

B)  $(0, 3)$

C)  $(-\infty, 3)$

D)  $(3, \infty)$

5) Let  $f(x) = \frac{2}{x-6}$  and  $g(x) = \frac{x}{x+1}$ , then the domain of  $(f+g)(x)$  is:

A)  $(-1, 6)$

B)  $\mathbb{R} - \{-1, 0, 6\}$

C)  $\mathbb{R} - \{-1, 6\}$

D)  $[-1, 6]$

You must write the correct answer to each question in the box below

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Answer					

6B)  $\left(\frac{x^{-6}y^4}{x^2y^{-1}}\right)^{-2} =$

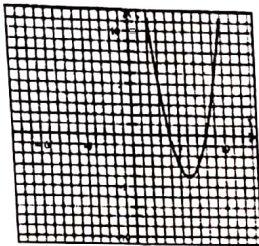
A)  $\frac{y^6}{x^8}$

B)  $\frac{x^{16}}{y^{10}}$

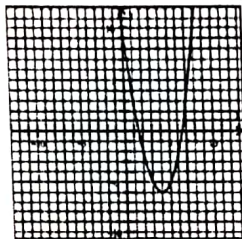
C)  $\frac{y^{10}}{x^{16}}$

D)  $\frac{x^8}{y^6}$

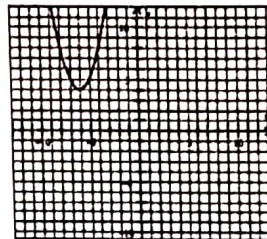
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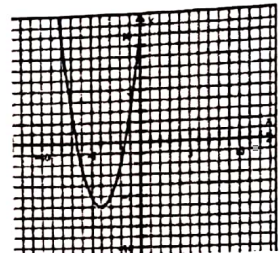
A)



B)



C)



D)

8) Find the **x-intercepts** of the graph of the equation:  $y = (x+4)^2 - 1$

A)  $\{-3\}$

B)  $\{-4, 1\}$

C)  $\{3, 5\}$

D)  $\{-5, -3\}$

9) Find the **distance** between the two points:  $(4, -6)$  and  $(5, 2)$

A) distance =  $\sqrt{65}$

B) distance =  $\sqrt{63}$

C) distance =  $\sqrt{97}$

D) distance =  $\sqrt{17}$

10) Find the equation of the circle with center  $(-2, 3)$  and radius 5

A)  $(x-2)^2 - (y+3)^2 = 25$

B)  $(x+2)^2 + (y-3)^2 = 25$

C)  $(x-2)^2 + (y+3)^2 = 25$

D)  $(x+2)^2 + (y-3)^2 = 5$

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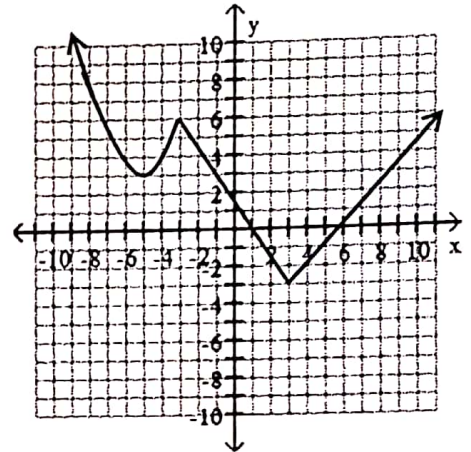
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- $f(6) =$



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- Find the vertex of  $f$
- Find the  $x$ -intercepts, if any
- Find the  $y$ -intercept
- Determine whether  $f$  has a maximum or a minimum
- Sketch the graph  $f$

