

Prince Sultan University **MATH 211** Final Exam First Semester 2007/2008, Term 081 Thursday, February 5 2009 Dr. Aiman Mukheimer

## Time Allowed: 100 minutes

(Middle)

(Last)

ID Number:

## **Important Instructions:**

- You may use CASIO scientific calculator that does not have programming or graphing capabilities.
- You may **NOT borrow** a calculator from anyone.
- There should be **NO talking** during the examination.
- Your exam will be taken immediately without any warning if your mobile is seen or heard
- You must show all your work beside the problem. Be organized.
- You may use the back of the pages for extra space, but be sure to indicate that on the page with the problem.
- This examination has 10 problems, some with several parts. Make sure that your paper has all these problems

Problems	Max points	Student's Points
1,2,3	17	
4,5	14	
6	12	
7	20	
8,9,10	17	
Total	80	

**Q1.** (6 points) How long will it take for an amount of \$6195 reach \$10000, with an interest rate 6% compounded monthly.

**Q2.** (6 points) It is estimated that t months from now the population of a certain town will be changing at the rate of  $4+5t^{\frac{2}{3}}$  people per month. If the current population is 10,000, what will be the population 8 months from now?

**Q3.** (5 points) The total cost of producing x units of a certain commodity is  $C(x) = x^2 - 5x + 8$ . Determine the minimum cost of the commodity.

**Q4.** (7 points) Find the critical points of  $f(x) = \frac{x^2}{x-2}$  and use the second derivative test to classify each critical point as a relative maximum or minimum.

**Q5.** (7 points) Sketch the region *R* and then find the area bounded by the *x* – axis and the curve:  $y = -x^2 + 4x - 3$ 



**Q6.** (12 points) Use calculus to sketch the graph of the function  $f(x) = 3x^5 - 20x^3$ 



**Q7.** (20 points) Evaluate the following integrals: -3

$$1. \int \frac{(\sqrt{x}-1)^{\frac{2}{2}}}{\sqrt{x}} dx$$

2. 
$$\int_{0}^{6} x^{2}(x-1) dx$$

$$3. \int_{-1}^{4} \frac{x}{\sqrt{x+5}} dx$$

$$4. \int \frac{x^3}{\sqrt{x^2 + 1}} dx$$

**Q8.** (5 points) Evaluate the partial derivative  $f_x(1,1)$  for the function

$$f(x, y) = xy \ln\left(\frac{y}{x}\right) + \ln\left(2x - 3y\right)^2$$

**Q9.** (6 points) Records indicate that *t* months after the beginning of the year, the price of ground beef in local supermarkets was  $P(t) = 0.09t^2 - 0.2t + 1.6$  dollars per pound. What was the average price of ground beef during the first 3 months of the year?

**Q10.** (6 points) Describe and sketch the <u>domain</u> for the following functions:

1. 
$$f(x, y) = \frac{4x - 8e^{y}}{(-x^{2} - y^{2} + 9)^{1/2}}$$
  
2.  $f(x, y) = \ln(4 - y)$