

Prince Sultan University MATH 113

First Examination First Semester 2014/2015, Term 141 Wednesday, 22nd October 2014

Dr. Bahhaeldin Abdalla & Dr. Ahmed Kaffel

Time Allowed: 70 minutes *Maximum points: 30 points*

N.T.	TD N. 1 "
Name:	ID Number #

Important Instructions:

- 1. You may use CASIO scientific calculator that does not have programming or graphing capabilities.
- 2. You may NOT borrow a calculator from anyone.
- 3. You do NOT get special consideration if you forget your calculator.
- **4.** Don't use notes or any notebook.
- 5. There should be NO talking during the examination.
- **6.** Your exam will be taken immediately without any warning if your mobile is seen or heard.
- 7. You must show all your work beside the problem. Be organized.
- 8. You may use the back of the pages for extra space, but be sure to indicate that on the page with the problem.
- **9.** This examination has 9 problems, some with several parts. Make sure that your paper has all these problems

Problem	Max points	Student's Points
1,2	9	
3,4,5	7	
6,7	7	
8,9	7	
Total	30	

1. (6 points) Evaluate each integral.

(a)
$$\int \frac{t^3}{1+t^4} dt$$

(b)
$$\int \frac{x}{x^4 + 1} dx$$

(c)
$$\int \frac{\sqrt{y} - y}{y^3} dy$$

2. (3 points) The velocity function for a particle moving along a line is given by v(t) = 3t - 5. Find the distance traveled by the particle between t = 0 and t = 3.

3. (3 points) Use the properties of integrals to estimate the integral and to determine *a* and *b*.

$$a \le \int_{-1}^{1} \sqrt{2 + x^2} dx \le b$$

4. (2 points) Estimate the area under the graph of $f(x)=1+x^2$ from x=-1 to x=5 using 3 rectangles and right endpoints.

5. (2 points) Find the derivative of the function $h(x) = \int_{1}^{\sqrt{x}} \frac{z^2}{z^4 + 1} dz$.

6. (3 points) Find the area enclosed by the line y = x - 3 and the parabola $y^2 = 2x + 2$.

7. (4 points) Find the volume of the solid obtained by rotating the region bounded by $y = (x-2)^2$ and y = 4 about the x-axis.

8. (4 points) Use the method of cylindrical shells to find the volume generated by rotating the region bounded by $x = y^2 + 1$ and x = 2 about the line y = 2.

9. (3 points) Find the average value of the function $f(\theta) = \sec^2\left(\frac{\theta}{2}\right)$ on $\left[0, \frac{\pi}{2}\right]$.