

Q1 (pts) A hospital spokesperson reported that 4 births had taken place at the hospital during the last 24 hours. We consider only the gender of these four children, recording M for a male child and F for a female. There are 16 gender combinations possible.

(a) List these 16 outcomes in terms of simple events beginning with E_1 as (FFFF)

(b) Define following events in term of simple events

A: No girl is born, B: Two boys and two girls are born,

C: At least one girl is born D :Three boys and one girl is born.

(c) Find $P(A \cap B)$, $P(B \cap C)$, $P(A \cup D)$ and $P(C)^c$

(d) Calculate $P(A | C)$ and $P(D | C)$.

Q2 (pts) Fill in the blanks for given table

P(A)	P(B)	Conditions for events A and B	$P(A \cap B)$	$P(A \cup B)$	$P(A B)$
.3	.4	mutually exclusive			
.3	.4	Independent			
.1	.5				.1
.2	.5		0		

Q3 (pts) Given sample space $S = \{ E_1, E_2, E_3, E_4, E_5, E_6, E_7 \}$
 Event $A = \{ E_1, E_3, E_5, E_7 \}$ Event $B = \{ E_2, E_3, E_4, E_5 \}$
 Draw two Venn diagrams for (a) $A \cap B$ (b) B^c . Shade the desired area,
 Indicating positions of all elements.

Q4(pts) Let X be a discrete random variable with a probability distribution given as

X	-2	-1	0	1
$P(x)$	$\frac{1}{9}$	$\frac{1}{9}$	$\frac{4}{9}$	-

(a) Find $P(1)$ (b) Find mean $= E(X)$ (c) Find standard deviation of X

Q5 (pts) Suppose a particular set of symptoms denoted as event H , occurs only when any one of these illnesses A , B or C occurs. Assume that illnesses A , B , and C are mutually exclusive.

Studies show these probabilities of getting the three illnesses

$P(A) = 0.01$, $P(B) = 0.005$, $P(C) = 0.02$. the probabilities of developing the symptoms H , given a specific illness $P(H | A) = 0.90$, $P(H | B) = 0.95$, $P(H | C) = 0.75$, assuming that an ill person shows the symptoms. What is the probability that person has illness A . What is the probability that person has illness C .

Q6 A Sociologist is interested in drawing a random sample of six individuals from a group consisting

of 9 males and 8 females.

(a) How many different samples of size 6 are possible?

(b) How many samples would consist of all males ?

(c) How many samples would consist of 3 males and 3 females

(d) Find the probability that the sample contains three males and 3 females.

Q7 (4 pts) Let X be a Binomial random variable with $n=7$ and $p=0.3$, Find these values

(a) $P(X=4)$, (b) $P(X=1)$, (c) $P(X=1)$, (d) mean (e) standard deviation